

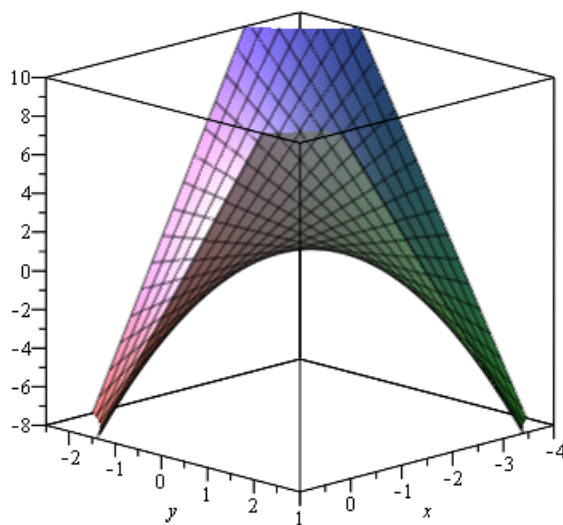
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> restart; with(plots):
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Pr. 0, soustava dvou lin. rovnic, jeden stacionární bod

$$z0 := 2xy - x + 3y$$

$$x = -\frac{3}{2}, y = \frac{1}{2}, \text{sedlo}$$

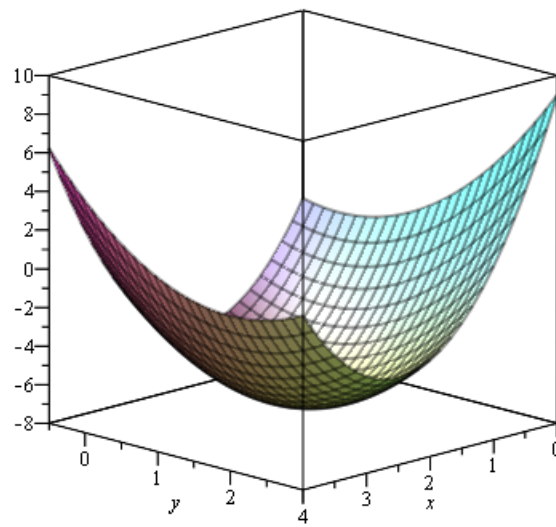


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Pr. 1, soustava dvou lin. rovnic, jeden stacionární bod

$$z1 := 2x^2 + y^2 - xy - 7x$$

$$x = 2, y = 1, f_{\min} = -7$$

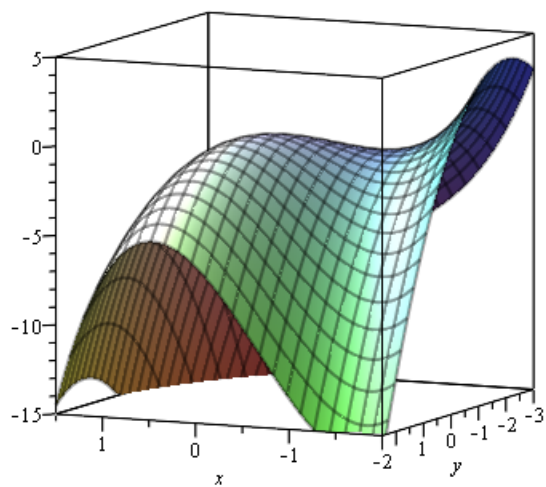


Pr. 2, soustava lin. a kvadr.rovnice, bez absol.lenu, dva stacion. body

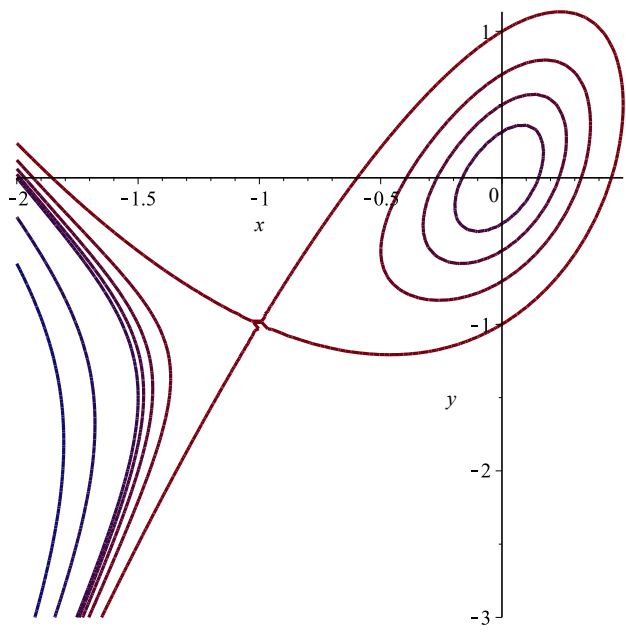
$$z := 2xy - 2x^3 - 4x^2 - y^2$$

$$x=0, y=0, f_{\max}=0$$

$$x=-1, y=-1, \textit{sedlo}$$



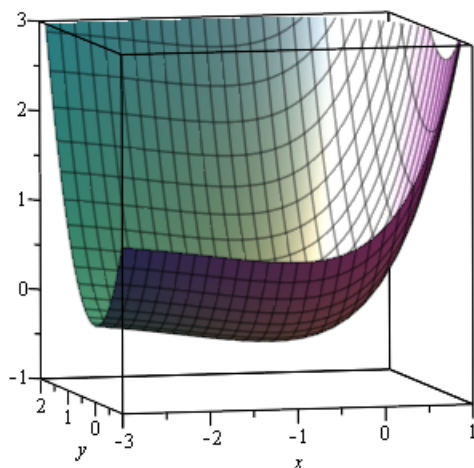
# Izokivky



Pr. 3, dv samostatné rovnice (jedna lin., jedna s exp.), jeden stac. bod

$$z3 := x e^x + y^2$$

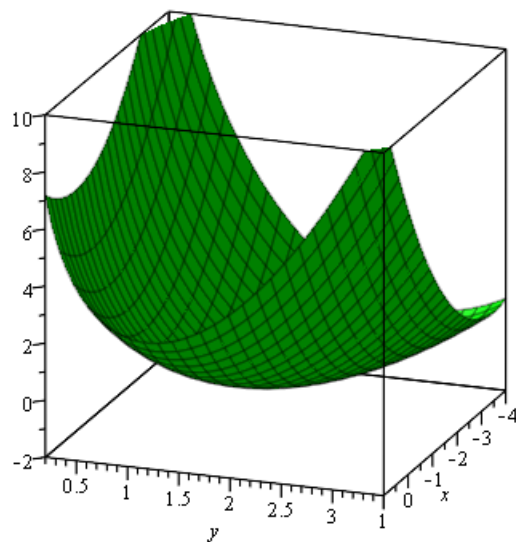
$$x = -1, y = 0, f_{\min} = -\frac{1}{e}$$



Pr. 4, jeden stacionární bod, POZOR:  $[2,-2]$  nepatí do def. oboru !

$$z_{ZkA} := 0.5 x^2 + x y + y^2 - 4 \ln(y)$$

$$x = -2, y = 2, f_{\min} = 2 - 4 \ln(2)$$

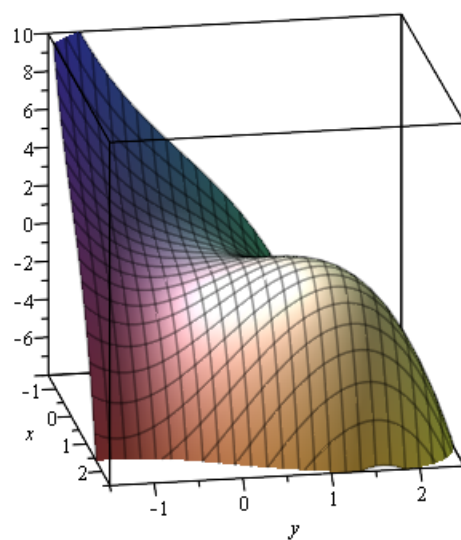


Pr. 5, soustava dvou kvadratických rovnic, dva stacion. body

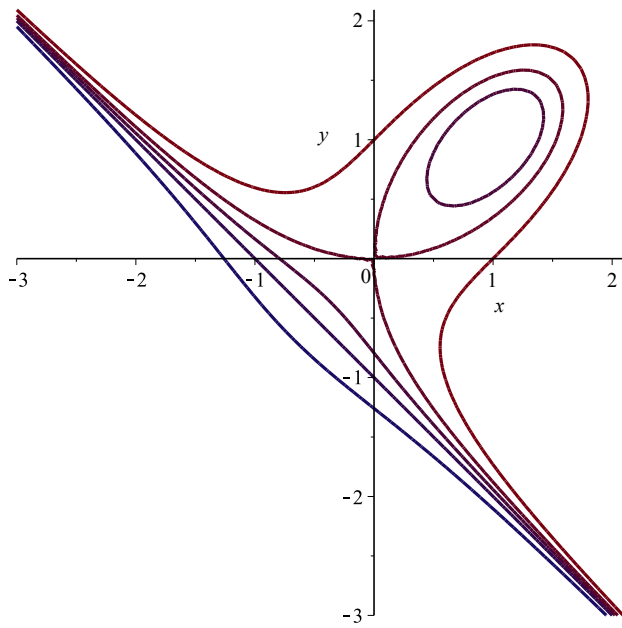
$$z_{5ZkA} := 3xy - x^3 - y^3$$

$$x = 1, y = 1, f_{\max} = 1$$

$$x = 0, y = 0, \textit{sedlo}$$



# Izokivky



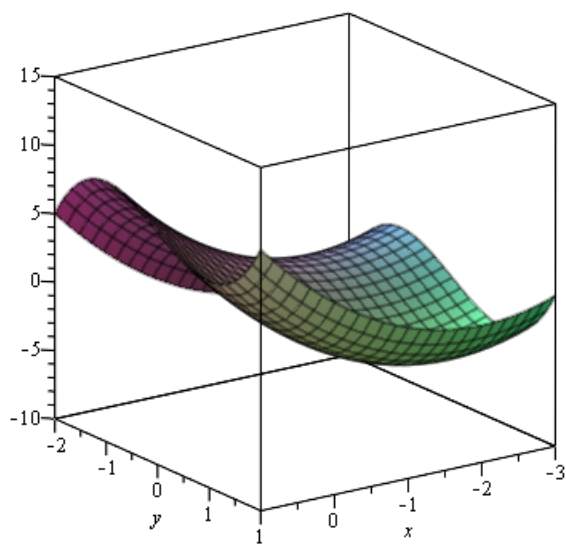


Pr. 6, dv samost. rovnice (lineární, kvadr.), dva stacion. body

$$z6 := x^2 + y^3 + 4x - 3y + 2$$

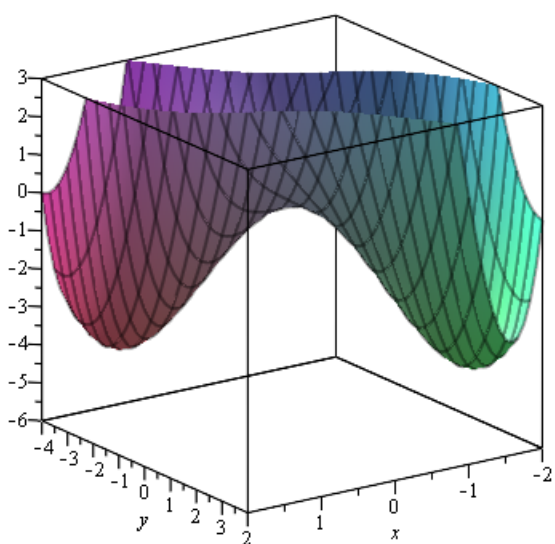
$$x = -2, y = 1, f_{\min} = -4$$

$$x = -2, y = -1, \textit{sedlo}$$



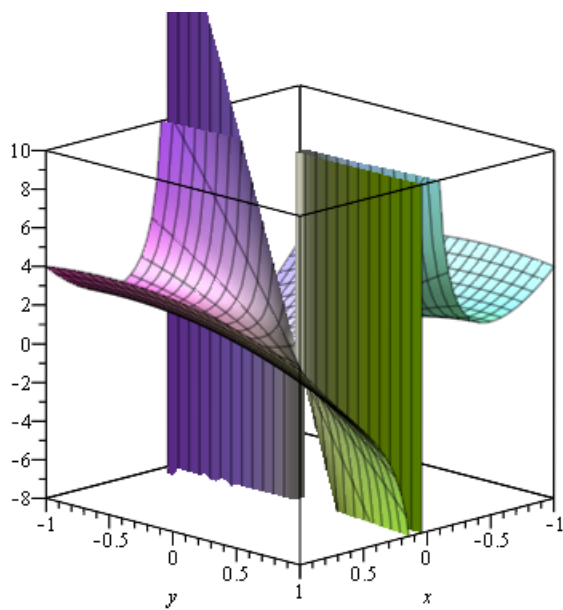
Pr. 7, ti stacionární body

$$z_7 := x^4 + 4xy + y^2$$
$$x = \sqrt{2}, y = -2\sqrt{2}, f_{\min} = -4$$
$$x = -\sqrt{2}, y = 2\sqrt{2}, f_{\min} = -4$$
$$x = 0, y = 0, \textit{sedlo}$$



Pr. 8, dva stacion. body:  $[1/2, -1]$ ,  $[-1/2, 1]$ . Oba jsou sedlové body, žádný extrém.

$$z_8 := 4x^2 - y^2 - \frac{y}{x}$$



Pr. 9, jeden stacionární bod

$$z_9 := y\sqrt{x} - y^2 - x + 9y$$

$$x=9, y=6, f_{\max}=27$$

